

Chapter 01. FUNCTIONS AND LIMITS

1) The domain of binary relation $y^2 = -4x$ is,

- A) \mathbb{R}
- B) \mathbb{Z}
- C) \mathbb{R}^+
- D) Negative real numbers including zero.

Answer: D

2) If $S = \{a, b, c\}$ then the number of distinct relations on S is

- A) 9
- B) 2^9
- C) 2^3
- D) 9^2

Answer: B

3) The domain of the binary relation $2x^2 + 2y^2 = 18$ is

- A) \mathbb{R}
- B) \mathbb{R}^+
- C) \mathbb{Z}
- D) $\{-3, 3\}$

Answer: D

4) The range of the binary relation $4x^2 + 9y^2 = 36$ is

- A) $\{-2, 2\}$
- B) $\{-3, 3\}$
- C) $\{-2, 3\}$
- D) \mathbb{R}

Answer: A

5) If $R_1 = \{(x, y) \mid x, y \in \mathbb{R} \text{ and } x > y\}$ is a binary relation then its inverse is

- A) $\{(1, 2), (2, 3)\}$
- B) $\{(2, 1), (3, 2), (4, 3)\}$
- C) $\{(x, y) \mid x = y\}$
- D) $\{(x, y) \mid x, y \in \mathbb{R} \text{ and } y > x\}$

Answer: D

6) The graph of the binary relation $y = x^2 - 6x + 5$ represents

- A) Line
- B) Circle
- C) Parabola
- D) Ellipse

Answer: C

7) The graph of $R_1 = \{(x, y) \mid x, y \in \mathbb{R} \text{ and } y > x\}$ is

- A) Line
- B) Points on the line $y = x$
- C) All points below the line $y = x$
- D) All points above the line $y = x$

Answer: D

8) If $f(x) = ax + b$, where $a, b \in \mathbb{R}$, $a \neq 0$, then f is called a

- A) Constant Function
- B) Linear Function
- C) Quadratic Function
- D) Polynomial Function

Answer: B

9) The graph of a linear function represents a

- A) Circle
- B) Line
- C) Parabola
- D) Ellipse

Answer: B

10) The equation having null set as its solution set is

- A) $x = \cos x$
- B) $x = e^x$
- C) $x = \sin x$
- D) $x = \tan x$

Answer: B

11) The composition of two functions f and g is defined as $(f \circ g)(x) = f\{g(x)\}$, for all x in the set

- A) R_g
- B) D_g
- C) $D_g \cap D_f$
- D) $R_g \cap D_f$

Answer: D

12) If $f(x) = x$ and $g(x) = x^2$ then the value of $(f \circ g)(x)$ is

- A) x^2
- B) x
- C) x^3
- D) x^4

Answer: A

13) Let $f: S \rightarrow T$ be a one-to-one function such that $f(x_1) = 6$ and $f(2) = 6$ then the value of x_1 is :

- A) 6
- B) 2
- C) 3
- D) 12

Answer: B

14) Let $f(x) = 5x + 3$ then f is

- A) One-to-one function
- B) Onto function
- C) Constant function
- D) Both one-to-one and onto function

Answer: D

15) Let $f: S \rightarrow S$ be an identity function and $2 \in S$, then the value of $f(2)$ is

- A) 2
- B) -2

- C) 3
D) $\frac{1}{2}$
Answer: A
- 16) Let $g = \{(1, 1), (2, 3), (3, 2), (4, 4)\}$ be a function from S onto S, then the value of $g^{-1}(2)$ is,
A) 2
B) 3
C) 4
D) 1

Answer: B

- 17) Let $f(x) = 5x + 1$, $x \in \mathbb{R}$ then value of $f^{-1}(6)$ is,
A) 31
B) 1
C) 6
D) $\frac{1}{6}$

Answer: B

- 18) If $g(x) = 2x + 1$ then the value of $g^2(1)$ is
A) 3
B) 9
C) 7
D) 8

Answer: C

- 20) The graph of the function $y = x$ and $y = \tan x$ intersect at the point
A) $x = \pi/4$
B) $x = 0$
C) $x = \pi/2$
D) $x = \pi/3$

Answer: B

- 21) The solution set of the equation $x = \tan x$ is
A) ϕ
B) $\{\pi/4\}$
C) $\{1\}$
D) $\{0\}$

Answer: D

- 22) The solution set of $2x^3 - 3x^2 + 4x - 5 = 0$ can have at the most,
A) 4 members
B) 3 members
C) 2 members
D) 5 members

Answer: B

- 23) If $f(x) = 2x^2 - 1$ and $g(x) = 5x + 2$ then value of $f[g(2)]$ is
A) 312
B) 87
C) 287
D) 288

Answer: C

- 24) The inverse function of the function
 $y = \frac{x-1}{x+1}$, $x \neq -1$ is

A) $f^{-1}(y) = \frac{y+1}{y-1}$

B) $f^{-1}(y) = \frac{1-y}{1+y}$

C) $f^{-1}(y) = \frac{1+y}{1-y}$

D) $f^{-1}(y) = \frac{1-y}{y-1}$

Answer: C

- 25) If $y = \frac{x}{x+2}$, $x \neq -2$ is a function then the value of $f^{-1}(2)$ is, (Here $y = f(x)$)
A) $\frac{1}{2}$
B) 4
C) $\frac{1}{4}$
D) -4

Answer: D

- 26) If x & y are not separable, then it is called _____ function.

- A) $\lim h(x) = L$
B) Even
C) Implicit
D) Odd

Answer: C

- 27) **If the degree of a polynomial function is 1, then it is called a _____ function.**
A) Non linear
B) linear
C) Even
D) Odd

Answer: B

- 28) **The term function was recognized by a German Mathematician _____.**

- A) Euler
B) Leibniz
C) Pythagoras
D) Boyle

Answer: B

FUNCTIONS ON \mathbb{N} PORTION

- 1) The nth term of 3,9,27, ... is
A) 9^n
B) 3^n
C) 3^{n+1}

D) 3^{2n-1}
Answer: B

2) First three terms of the sequence whose n th term is $\frac{1}{3n+1}$

- A) $\frac{1}{4}, \frac{1}{5}, \frac{1}{6}$
- B) $\frac{1}{4}, \frac{1}{5}, \frac{1}{7}$
- C) $\frac{1}{4}, \frac{1}{7}, \frac{1}{10}$
- D) $\frac{1}{2}, \frac{1}{5}, \frac{1}{6}$

Answer: C

3) If $a_n = n+1$ and $b_n = \frac{1}{n+1}$, then n th term of the sequence $a_n b_n$ is

- A) $n^2 + 2n + 1$
- B) $n+1$
- C) 1
- D) $2n+1$

Answer: C

4) Limit of the sequence whose general term is $\frac{n^2+1}{n^2-1}$

- A) 2
- B) 3
- C) 4
- D) 1

Answer: D

5) All the sequences are the function whose domain is the set of

- A) irrational number
- B) Imaginary number
- C) Natural number
- D) Whole number

Answer: C

6) $\lim_{n \rightarrow \infty} a_n =$

- A) $\lim_{n \rightarrow -\infty} a_n$
- B) $\lim a_n$
- C) $\lim_{n \rightarrow 0} a_n$
- D) None of these

Answer: B

7) The sequence 1,2,3,4, . . . is

- A) Monotonic increasing
- B) Monotonic decreasing
- C) maxima
- D) minima

Answer: A

8) The sequence $\frac{1}{2}, \frac{1}{3}, \frac{1}{4}, \dots$ is

- A) Monotonic increasing
- B) Monotonic decreasing
- C) Maxima
- D) Minima

Answer: B

9) The sequence $\frac{1}{3}, \frac{1}{9}, \frac{1}{27}, \dots$ is

- A) convergent
- B) divergent
- C) Maxima
- D) Minima

Answer: A

10) The sequence 4,16,64, . . . is

- A) convergent
- B) divergent
- C) Maxima
- D) Minima

Answer: B

11) The limit of a convergent sequence is _____.

- A) Unique
- B) Not unique
- C) Both A and B
- D) None of these

Answer: A

LIMIT OF A FUNCTION PORTION

1) $\lim_{x \rightarrow a} f(x) = h$ is read as

- A) limit of $f(x)$ is equal to h as x tends to a
- E) $f(x)$ limit x tends to a is h
- F) Limit $f(x)$ is equal to h
- G) All of these

Answer: A

2) $\lim_{x \rightarrow a} f(x) = h$ can be written as $f(x) \rightarrow h$ as $x \rightarrow a$ and us read as

- A) $f(x)$ tends to h as x tends to a
- E) limit of $f(x)$ is equal to h as x tends to a
- F) limit $f(x)$ is h
- G) none of these

Answer: A

3) $x \rightarrow a$ describes that x

- A) Is very close to a but not actually equal to a
- E) Approaches a or tends to a
- F) Both A and B
- G) None of these

Answer: C

4) $\lim_{x \rightarrow 0} \frac{\sin x}{x} = 1$, here x is measured in

- A) degree

- E) radian
- F) gradian
- G) all of these

Answer: B

5) $\lim_{x \rightarrow 2} \frac{x^2 - 4}{x - 2} =$

- A) 4
- E) 5
- F) 6
- G) 7

Answer: A

6) $\lim_{x \rightarrow 0} \frac{\tan x}{x} =$

- A) 2
- E) 3
- F) 4
- G) 1

Answer: D

7) $\lim_{x \rightarrow 0} \frac{\sin 5x}{\sin 7x} =$

- A) $\frac{25}{49}$
- E) $\frac{5}{7}$
- F) $\frac{1}{7}$
- G) $\frac{5}{17}$

Answer: B

8) $\lim_{x \rightarrow 1} \frac{x^3 - x}{x^2 - 1} =$

- A) 2
- B) undefined
- C) infinity
- D) 1

Answer: D

9) $\lim_{x \rightarrow 1} \frac{x+1}{x-1} =$

- A) undefined
- E) infinity
- F) Both A and B
- G) None of these

Answer: B

10) $\lim_{n \rightarrow \infty} \left(1 + \frac{1}{n}\right)^n =$

- A) Natural logarithm
- B) e
- C) e^2
- D) 1

Answer: B

11) $\lim_{n \rightarrow \infty} \left(1 + \frac{5}{n}\right)^n =$

- A) e^5
- E) e
- F) e^4
- G) none of these

Answer: A

12) Maclaurance series of e^x is

- A) $1 + x + x^2 + x^3 + \dots$
- B) $\frac{1}{0!} + \frac{x}{1!} + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots$
- C) $1 - x + x^2 - x^3 + \dots$
- D) All of these

Answer: B

13) $\lim_{x \rightarrow 0} \frac{e^x - 1}{x} =$

- A) 0
- B) 1
- C) 2
- D) infinity

Answer: B